



Introduction to Geometry

Remote Learning Packet for GLE 2–4



TEACHER'S GUIDE



Created with funding from the Adult and Community Learning Services division of the Massachusetts Department of Elementary and Secondary Education by the SABES Mathematics and Adult Numeracy Curriculum & Instruction PD Center, which is managed by TERC, Inc.

Rationale

This packet was developed and piloted for use with students who do not have access to computers or are unable to participate in other forms of remote or online learning. The activities are designed to be done together with a teacher on an audio call. There are also recommendations for ways to enhance the activities by texting photos or links between teacher and student, if this option is available.

The math content is aimed at ABE level math students (approximately GLE 2-4). To keep things accessible, the text is kept to a minimum so that this could be used with students at an ABE reading level or students who are beginning to intermediate English Language Learners.

Considerations

- ▶ **These materials are designed for a group of adult students who are the most likely to be left out during the COVID-19 switch to remote learning: students with limited academic skills and limited access to technology.** Keep in mind that academic progress may be slow, and that maintaining student engagement, connection, and motivation is just as important as academic outcomes during this time.
- ▶ The student packet and shape set can be mailed to students before instruction begins. Consider scheduling times for phone tutoring with students once or twice a week.
- ▶ Consider adding an alternative number to your cellphone that you use with students. You can get an alternative number for free with applications like Google Voice. This protects your personal contact information, and it also keeps your student correspondence in a separate place.
- ▶ While you are working with students, ask them about specific technology skills and capabilities. Can they receive a photo via text? Can they see the photo while they are on the phone with you? Do they know how to send a photo to you? If you text them a link, do they know how to open it? Do they have the data available to watch a video on their phone? When possible, help students build these skills.
- ▶ Given the format of delivery and student levels, the amount of time it takes to complete the unit may vary widely. Many of the concepts may be new to students at this level, so they may need repetition (with variation) of some activities. The activities are arranged in a suggested order in the Student Packet and Teacher's Guide, but teachers can choose to skip activities or reorder them as needed.

- ▶ It is helpful to take detailed notes of what you worked on with each student as you are on the phone or afterwards. When you have a number of different students working on the same packet, it is impossible to keep track of who has done what! These notes will be helpful later when you assess students for understanding both during and at the end of the unit.
- ▶ Students working remotely need even more regular feedback about their progress than in person. Consider sharing their progress at least biweekly so they can see themselves progressing through the unit. You can add your notes to the Progress Report for each student and send them a photo by text.

Preparation Suggestions

- ▶ There are some shape puzzles that use the Shape Set, so it is important that both the Shape Set and the Student Packet be printed true to size, so that the shapes will fit the puzzles. When printing the Shape Set PDF document, be sure to choose “Actual Size” in the Page Sizing & Handling print menu.
- ▶ The packets can be printed on ordinary paper. It is highly recommended that you use a brightly colored sheet of paper as a cover sheet. This makes it easier for students to keep track of the packet and makes it easy to refer to (“You will need your green packet”).
- ▶ Most of the activities work fine when printed in black and white. If possible, print out the Flag activity (page 13) in color if you can, so that you can refer to the shape in the flags by color.
- ▶ Print out the Shape Set on brightly colored paper as well. Cut out the shapes before mailing them if you think that cutting them would be a barrier for your students. You can also staple an extra copy of the shape set to the back of the packet in case students lose some of their shapes, which will probably happen at some point.
- ▶ Use the same color cover sheets, shape sets, envelopes, etc. for all students. This will save you a lot of confusion when you ask someone to get out their yellow shapes (but theirs are pink).
- ▶ Start collecting pictures on your phone of where you see shapes in your home and around your neighborhood. These will be useful examples to text to students when you are talking about different shapes.

Math Background: The Development of Geometric Reasoning

Just like other domains of mathematics, the study of geometry is about more than just acquiring knowledge. When we teach geometry, we are looking to provide students with the opportunity to develop geometric reasoning.

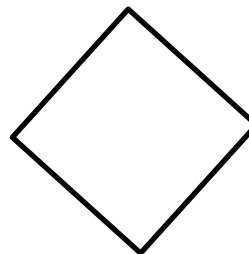
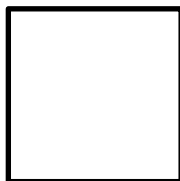
A pair of influential Dutch educators named Pierre van Hiele and Dina van Hiele-Geldof developed a model of the way in which students develop geometric thinking. Here are a few important things to know about their theory of the development of geometric reasoning:

- There are five levels of understanding spatial concepts.
- The levels are sequential; must pass through all prior levels to arrive at any specific level.
- The levels are not age-dependent. It is possible for adult students to be at any of the five levels, including the earliest (level 0).
- Geometric experiences have the greatest influence on advancement through the levels.
- Instruction and language at a level higher than the level of the student may inhibit learning.

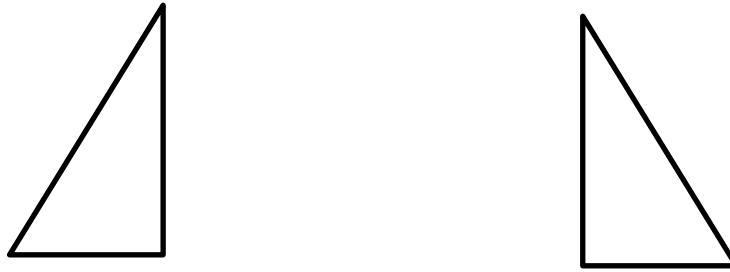
This curriculum is meant to provide geometric experiences for students in the first two levels of geometric reasoning.

Level 0: Visualization

At this level, students are developing an intuitive and sensory understanding of what different shapes “look like”. It is important for students at this level to have many concrete experiences with different ways that shapes can look: for example, they may not realize that the two shapes below are the same:



Or that some shapes can be flipped and be “different” (non-congruent).



Students need the concrete experience of manipulating shapes to develop this intuitive understanding. That is why the Shape Set is such a critical part of the curriculum – don't be tempted to skip it!

Many of the activities in the packet work on giving students at this level lot of experiences with the different ways that shapes can look, including the introductions to different shapes where they look for similarities and differences, shape puzzles, creating designs, and trying to identify shapes in real life objects.

Level 1: Analysis

At this level, students are paying more attention to the specific attributes of shapes and how these attributes define categories of shapes. For example, a student at this level will decide whether something is a rectangle based on whether it has right angles, and not just whether it “looks like” a rectangle.

This curriculum has students explore a few common attributes of shapes: angles (esp. right angles), parallel lines, and symmetry. For students at level 0, this will provide them with more concrete vocabulary to describe what they see in the shapes. For students at level 1, this will help them begin to think about more formal definitions of shapes and how shapes can be categorized, based on these attributes.

Higher levels of geometric reasoning start using both informal and formal methods of deduction and proof. Since this curriculum is intended for students at early levels of geometric reasoning, these types of tasks are not included.

This section is based on a summary of van Hiele's work found in Chapter 21 “Geometric Thinking and Geometric Concepts” in *Elementary and Middle School Mathematics: Teaching Developmentally, 4th ed.* (J.A. Van de Walle, Ed., 2001).

Concepts emphasized in this unit

Visualization and recognition of basic shapes

Many adult education students who lack concrete experiences with geometry and spatial reasoning still need to work visualizing shapes. This means recognizing what basic shapes can “look” like, for example that a rectangle can be both skinny or fat, or that a triangle can be even, or long and skinny, or irregular, and can point in any direction. Having the cut out shapes in the shape set is an important part of this because they can be rotated, flipped and manipulated.

Part of this visualization is also to get students looking for and recognizing shapes in their environment. The first time you ask, a student might say, “But there are no triangles in my house!” It is important to provide students with plenty of examples.

It is often easier for students to identify shapes when they are presented in a graphic, abstract form like the example on the right.



It can be more challenging for students to identify shapes that are created by objects in the environment, like in the example on the left.

Keep looking for shapes in your own environment so that you have plenty of examples to send to your students!

Identifying basic attributes of shapes

This unit presents students with a few important geometric concepts that are also attributes of shapes: angles (especially, right angles), parallel lines, and symmetry. Just like the shapes, these concepts need to be experienced as concretely as possible, so that students develop an intuition for what they look and act like. Angles are introduced using joints in the body, so that students can understand both visually and kinesthetically that an angle is an amount of opening or closing, like the way we can open or close our arm. Parallel lines are explored using long straight objects to extend sides into space. Symmetry is explored using folding and by looking at both symmetry and asymmetry in familiar objects.

If students have a hard time understanding how to manipulate the objects and shapes in these explorations, it can be helpful for you to send photos as examples. Starting photos and links to videos are also provided in the Student Packet and Teachers' Guide.

Composing and decomposing basic shapes

Composing and decomposing refers to putting shapes together to make new shapes, or breaking shapes apart into component shapes. Students explore composition and decomposition of shapes as they use their shape set to solve shape puzzles (similar to the popular game Tangrams) and create their own shapes. They also explore how everyday objects can be decomposed into basic shapes.

For example, the outline of this carton is a pentagon, but it can be decomposed into a triangle and rectangle.



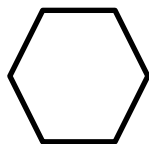
Pushing forward

A few of the activities push students to start to analyze shapes at a more abstract level, using specific characteristics and definitions to identify or sort shapes (*Square and Rhombus, Is It a Rectangle?, Compare Shapes, Sort Shapes*). These come later in the packet after students have had a chance to explore visualizations of shapes in the earlier activities.

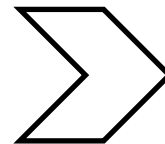
Teacher Cheat Sheet: Shapes and Their Attributes

Note: The shapes in this unit are all convex forms of the shape, meaning none of the internal angles are more than 180°

convex hexagon



concave hexagon



Most of the definitions of these shapes do not require that the sides be of equal length. When the sides are equal, the shapes are called "regular". For example, the convex hexagon above is a regular hexagon.

Shapes and Their Attributes			
Shape Name	Definition (Essential Attributes)	Familiar Examples	Notes
Rectangle	Four sides Two pairs of opposite sides of equal length Opposite sides parallel Four right angles	Cell phone Computer screen Door Window Table Paper	Rectangles are an important foundational shape for students to understand. Make sure they can see examples of “fat” and “skinny” rectangles, as well as rectangles in different orientations.
Square	Four equal sides Four right angles A square is both a rectangle and a rhombus (a special case of each).	Floor tiles Napkins Coasters CD case Holes in a chain link fence	Students often do not recognize a square turned on its side (“diamond”)
Triangle	Three sides (Because that is the only requirement, triangles can vary widely in other attributes)	Often seen on bridges Clothes hangers Objects leaning against a wall	Triangles are an important shape because all other polygons can be broken (decomposed) into triangles
Trapezoid	Four sides Exactly one pair of parallel sides	Lamp shade Glass lamp Window Pedestal	Trapezoids can have right angles (or not) and can be symmetrical (or not)
Pentagon	Five sides	House Home plate Crossing sign	
Hexagon	Six sides	Cereal Tea bag Bolt and nut	Regular hexagons (equal sides and angles) can tile, that is, cover a surface without leaving gaps.
Octagon	Eight sides	Stop sign	
Rhombus	Four equal sides (a square is a special rhombus with right angles)	Diamond shape	

Introduction to Geometry		Unit Plan
Prior Knowledge	<ul style="list-style-type: none"> • Reading level GLE 2 • Ability to communicate with teacher over the phone 	
Math Concepts Addressed	<ul style="list-style-type: none"> • Visualization and recognition of basic shapes • Identifying basic attributes of shapes, including angles, parallel lines, and symmetry • Composing and decomposing shapes • Beginning to categorize shapes by their attributes and to identify shapes based on definitions 	
CCRS/SAE Standards	<ul style="list-style-type: none"> • Analyze, compare, create, compose shapes. (K.G.4) • Reason with shapes and their attributes. (1.G.2, 2.G.1, 3.G.1) • Draw and identify lines and angles, and classify shapes by properties of their lines and angles. (4.G.1) 	
Materials Needed	<ul style="list-style-type: none"> • Students will need to receive a copy of the Student Packet and the Shape Set ahead of time. It is recommended that you include an extra copy of the shape set at the back of the packet. It is also helpful if students have a pair of scissors for one of the symmetry activities. • Teachers will need their own copy of the Student Packet, Shape Set, and Teachers' Guide, and one copy of the Progress Report for each student. 	
Vocabulary list of math terms	<i>geometry</i> <i>shape</i> <i>side</i> <i>angle</i> <i>rectangle</i> <i>trapezoid</i> <i>triangle</i> <i>square</i>	<i>right angle</i> <i>parallel</i> <i>symmetry / symmetrical</i> <i>line of symmetry</i> <i>pentagon</i> <i>hexagon</i> <i>octagon</i> <i>rhombus</i>

Introduction / Pre-Assessment

Introduction (page 1)

- 1) Explain to students that they will be studying geometry. Have them read the definition on page 1. Explain that while there are numbers and measurements in geometry, some of the work they will be doing will involve analyzing pictures, shapes, and space, and that this is an important part of mathematics. Give some examples of how geometry is used in the real world: design, building, engineering, home improvement, event planning, etc.
- 2) Go over the two words “side” and “angle” on the first page. Make sure students understand what these words refer to on a shape. Ask them to tell you how many sides and angles there are in the shapes A-C on the page. It is ok to use the word “corner” as well, to help students understand that in a shape, angles make corners.

Pre-Assessment (Shape Set)

- 1) Ask students if they have studied geometry before. Have them take out their shape set and make sure that they have twelve shapes. Ask them to tell you what they know about any of the shapes. You can ask probing questions, such as:
 - ▶ *Do any of these shapes look familiar?*
 - ▶ *Do you know the names of any of these shapes?*
 - ▶ *Can you think of anything in the real world that looks like one of these shapes?*

If students identify any of the shapes by name (correctly or incorrectly), you can ask:

- ▶ *How do you know that is a [rectangle]?*

Take notes on what students tell you.

Activities**Rectangles (page 2-3 & Shape Set)**

- 1) Explain that the shapes on this page are all rectangles. Ask students what they notice about the shapes and what they have in common. They can write this in the first box. Make sure they notice the number of sides and angles, and something about opposite sides being equal, however they choose to describe that. You don't have to go into right angles yet if they don't have that concept.
- 2) Also ask students what they see that is different between the shapes. They don't have to write this down, but point out that although some of the rectangles are skinny, other are fat, some are oriented vertically and others across, they are all rectangles.
- 3) Ask students to brainstorm *What has this shape in real life?* If they have a hard time, give them some examples that you see in the room around you.
- 4) Students may point out that C is a square. Affirm that yes, C is a square, and ask them how they know, or what makes it look like a square. Explain that a square is a special type of rectangle where all the sides are the same length. They will look at squares in more detail later.
- 5) Ask students to find the rectangles in the Shape Set (#1 and #3). They can label these shapes with the word "rectangle."
- 6) On the next page, *Find the Rectangles*, ask students to identify objects that they see in each picture that are rectangles.
- 7) **Homework:** Ask the student to text you a photo of something in their house that is a rectangle.

Angles in the Body (page 4)

- 1) Explain that one way to think about angles is that our body makes angles when we bend our joints. For example, our arm makes angles when we bend our elbow. The angle is the corner, like the corner in a shape. We measure how small or large an angle is by how open it is. When our arm is bent sharply, so that our elbow sticks out, the angle is small because the arm is only open a little bit. When we stretch out our arm so the elbow is only bent slightly, the angle is larger.
- 2) Explain that there is a special type of angle called a right angle. Make sure to point out that while we call this angle "right", it doesn't have to do with right or left, and it doesn't mean that other angles are wrong. The word "right" has a special meaning in math when we talk about angles.

- 3) To make this special angle with your arm, make your upper arm flat, and let your hand and fingers point straight up to the sky. This is a right angle. A right angle looks like the corner of a rectangle.
- 4) Draw their attention to the two pictures at the bottom. Which joints are making right angles? Point out that the right angle can point in any direction, as long as it is open the same amount as the angle we made with our hand pointing up.
- 5) Revisit the rectangles on page 2. Ask:
 - ▶ *Are all the angles right angles? How do you know?*

Right Angles: Paper Test (page 5 & Shape Set)

- 1) Another way of testing for right angles is to use the paper test. It might be helpful to send students a link to this video ahead of time:
- 2) Explain that regular paper is cut so that all the corners are right angles. We can use a piece of paper to test whether something has a right angle or not. We put the corner of the paper into the corner of the angle. If it fits perfectly, then the angle is a right angle.
- 3) Have students use the corner test on the angles A-D to decide if they are right angles.
- 4) Have students use the paper test to find right angles in the Shape Set.

Trapezoids (pages 6-7)

- 1) Follow the procedure used in Activity I, Rectangles. If students don't point it out, ask them if they see any right angles (B has two right angles. Some of the others are close, but they should check with the paper test.)
- 2) Students may not have the vocabulary to talk about parallel lines yet. That will be addressed in the next activity.
- 3) Ask students to look for trapezoids in the Shape Set (#10). They should label this shape.
- 4) On page 7, have students match which of the trapezoids at the bottom can be seen in each photo.
- 5) **Homework:** Ask the student to text you a photo of something in their house that is a trapezoid. If they cannot find a trapezoid, they should make one using pencils or other objects with straight edges.

Parallel or Not? (page 8)

- 1) Explain that parallel lines are lines that will never meet. Make sure students understand that it is not about whether we see them meet or cross on the page or in the shape, but about whether that would ever cross if they were extended.

Checking for Parallel Lines (page 9-10)

- 1) This page shows an example of using spaghetti to check whether lines in a shape are parallel. If students don't have spaghetti, they can use pens or coffee stirrers or anything long and skinny and straight.
- 2) After students understand how to check for parallel lines, have them practice by looking for parallel lines in the shapes of the Shape Set.
- 3) The following page, *Parallel Lines at Home*, also has examples of what parallel lines might look like in the real world.
- 4) Lastly, return to the *Rectangles* and *Trapezoids* pages. Ask:
 - ▶ Where do parallel lines appear in these shapes?

Triangles (page 11)

- 1) Follow the procedure used in the *Rectangles* activity.
- 2) If students don't point it out, ask them if they see any right angles (D has a right angle. They should check with the paper test.)
- 3) Extension question (students can explore this question with spaghetti or pens, or by drawing):
 - ▶ *Do you see parallel lines in any of the triangles? Is it possible to have parallel lines in a triangle? Why or why not?*
- 4) Ask students to look for triangles in the Shape Set (#2, 5, 6, 8). They should label these shapes.
- 5) **Homework:** Ask the student to text you a photo of something in their house that is a triangle. If they cannot find a triangle, they should make one using pencils or other objects with straight edges.

Triangles: Same and Different (page 12)

Have students fill in the two columns with what is the same about the two triangles, and what is different. Push them to use the vocabulary and concepts that they have been learning when appropriate, such as side, angle, right angle.

Flags (page 13)

- 1) Ask: *What shapes do you see in these flags?* When they identify shapes, ask them how they know that it is a [triangle].

You can also do this activity with a flag that is meaningful to the student. Text them a picture (look it up in Wikipedia and take a screen shot) and discuss the picture together.

- 2) **Homework Extension:** Have students design their own flag. Their flag should include at least three different types of shapes. They can text you a photo of their flag when finished.

Who Am I? (Shape Set)

- 1) You can play this game repeatedly throughout the unit. Model being the clue giver first, then take turns being the one giving clues.
- 2) One person chooses a shape from the shape set. They then give a clue about the shape. The other person then makes a pile of all the possible shapes that fit that clue. Then the clue giver gives another clue. Repeat until there is only one shape left and the person is ready to guess.
- 3) Another variation is to have one person pick a shape, and to have the other person ask yes or no questions about the shape.
- 4) As the teacher, model giving clues or asking questions about numbers of sides or angles, the existence of right angles, equal sides, or parallel lines. You can also give clues about objects in the real world that have this shape.

Dot Paper Activities Part 1

Below are two ideas for investigations you can have students do with the dot paper, included at the end of the student packet. This will work best if your student can send you photos of what they have done, so that you can see their work and discuss it with them.

To use the dot paper, students can draw lines connecting any dots on the page. They cannot draw curved lines. They cannot draw lines that do not connect dots.

More accessible:

- 1) Create three different rectangles (on square or triangle dot paper). Explain how they are different.
- 2) Create three different triangles (on square or triangle dot paper). Explain how they are different.

More Challenging:

- 1) Create four different four-sided shapes. At least three cannot be a rectangle. Describe how they are different.
- 2) Create a triangle with a right angle. Try to do this on the square dot paper and the triangle dot paper. Does it work on both?
- 3) Create a triangle with three sides of equal length. Try to do this on the square dot paper and the triangle dot paper. Does it work on both?

Making Symmetrical Shapes (page 14-15)

- 1) If possible, have students cut out their own symmetrical shapes following the example. Any shape they cut will be symmetrical with the fold as the line of symmetry.
- 2) Here is a link to a video demonstration you can text to students if they need more of a visual: Lines of Symmetry <https://youtu.be/BNfalGeUzzY>
- 3) Go over the definition of symmetry and the examples on page 15. Discuss the letter examples on the bottom to check for understanding.
- 4) **Homework:** Have students experiment with cutting folded paper to create symmetrical shapes. Can they create a shape that unfolds to make a heart? A star? A triangle? A rectangle? A donut? Have them send you pictures of the shapes they created. This can be a fun activity to do with kids if they have any at home.

Line of Symmetry (page 16)

- 1) Before working on this page, have students practice folding shapes in their Shape Set to check for symmetry. Discuss a couple of these examples. Are their shapes that have more than one line of symmetry?
- 2) The worksheet could be done together or assigned for homework. Encourage students to physically fold the page if they need to in order to visualize whether the shape is symmetrical. Make sure students are checking the line that is marked, as many shapes may be symmetrical across other lines.

Symmetrical or Not? (page 17)

These are more examples of human-made objects. Discuss with students whether each example is symmetrical (with a vertical line of symmetry). If it is not symmetrical, have them explain what details don't match.

Symmetry in Nature (page 18)

Explain that symmetry is very common in nature and natural objects. Ask them to think of other examples of symmetry in nature. (Another challenging question would be if they can think of animals that are NOT symmetrical in some way.)

Front and Side Views (page 19)

- 1) Explain that it is common for some objects to be symmetrical from one direction, and not symmetrical in the other. Discuss the examples on the page and whether each view is symmetrical or not.
- 2) Can students think of another object that is symmetrical from one direction, and not another? Can they think of an object (like the bird feeder) that is symmetrical from more than one view?

Finish the Shape (page 20)

Since you can't see what they are drawing, this would work best as a homework assignment. Students can send you a picture when they are finished.

U.S. Flag Review (page 21)

This is a quick review of concepts that have been studied so far. Ask:

- ▶ *What shapes do you see in this flag?*
- ▶ *What types of angles do you see?*
- ▶ *Do you see any parallel lines?*
- ▶ *Are there any lines of symmetry?*

Shapes with More Sides (page 22-23)

- 1) Give students the names and definitions of pentagons, hexagons, and octagons. Explain that these shapes are defined by the number of sides and angles, but the sides do not all have to be the same length. Have them write the letters of each shape in the appropriate box.
- 2) Where have they seen these shapes? Brainstorm, then have them look at the photos on the next page (*Shapes with More Sides: Examples*, page 23) for more ideas.

- 3) Find and label the pentagon (#12), hexagon (#7) and octagon (#11) in the shape set. Have the students turn the shapes around. Ask:
 - ▶ *Do they look different when you turn them? Do they look different when you flip them over?*
- 4) **Homework:** Have the student text you a photo of a pentagon, a hexagon, or an octagon. If they cannot find one, they should create one out of other objects or draw one on paper.

Which One Doesn't Belong? (page 24)

- 1) Like the *Same or Different* activity, this is an example of an open question. The goal is to have students provide a mathematical reason for their choice. There are many different arguments that could be made. For example:
 - A doesn't belong because it is the only shape where the sides are not all the same length.
 - B doesn't belong because it is the only shape that is shaded in (color is an attribute too!)
 - C doesn't belong because it is the only shape that points straight down.
 - D doesn't belong because it is the only shape with 5 sides (or with no right angles, or with no parallel lines).
- 2) Anything a student says is valid as long as it is true. Listen for gaps in understanding, such as if a student says that B is the only square (C is also a square). This type of activity can be good for a quick assessment to see what types of concepts your student is noticing and what type of math vocabulary they use.

Road Signs (page 25)

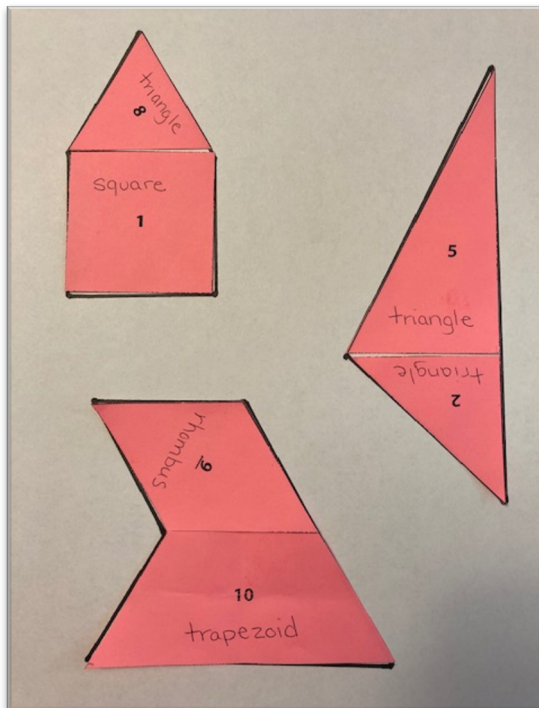
- 1) This is a nice way to review the shapes that have been learned so far. Students write the letter of the road signs that match each shape in the box.
- 2) This activity could be assigned for homework.

Shape Puzzles (page 26-31)

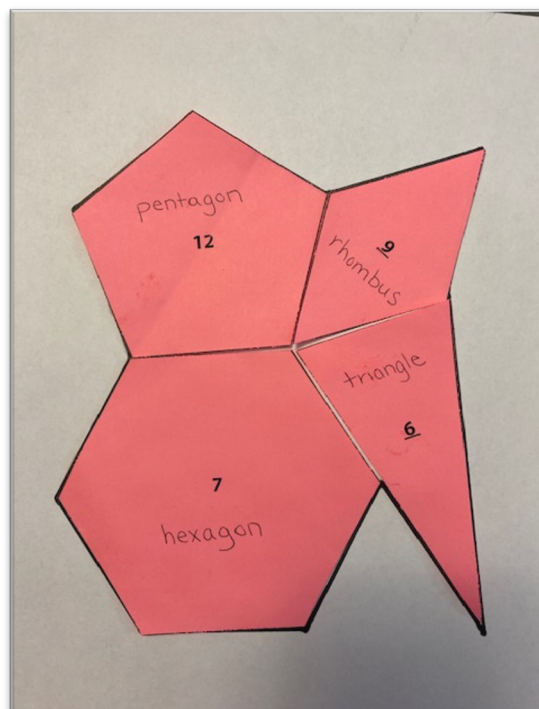
- 1) Explain that the shape puzzles can be built with shapes from the Shape Set (like the example). Not all the shapes will be used. Shapes can be turned or flipped over.
- 2) This is a good activity to assign for homework. Students can text you a picture of the finished puzzle.

Answer Key:

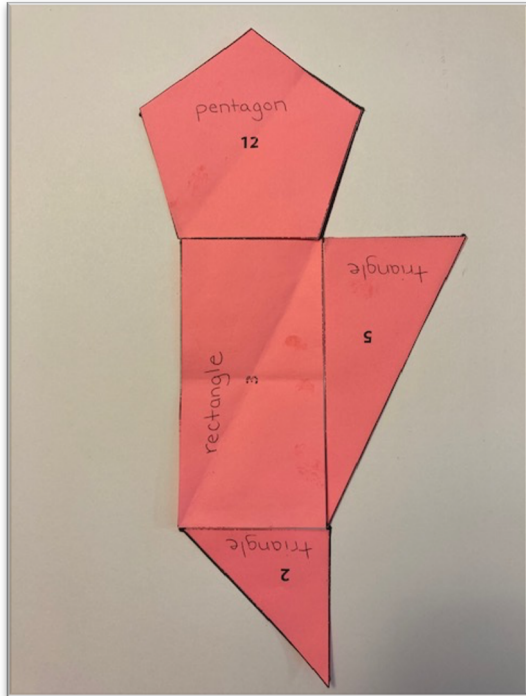
A - C



D

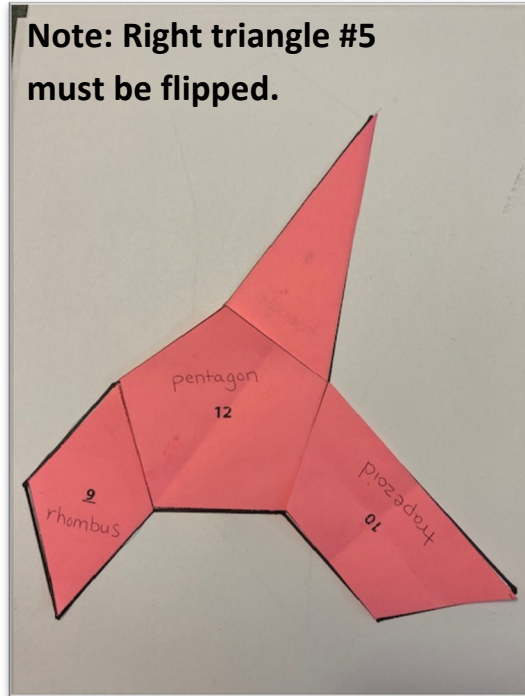


E

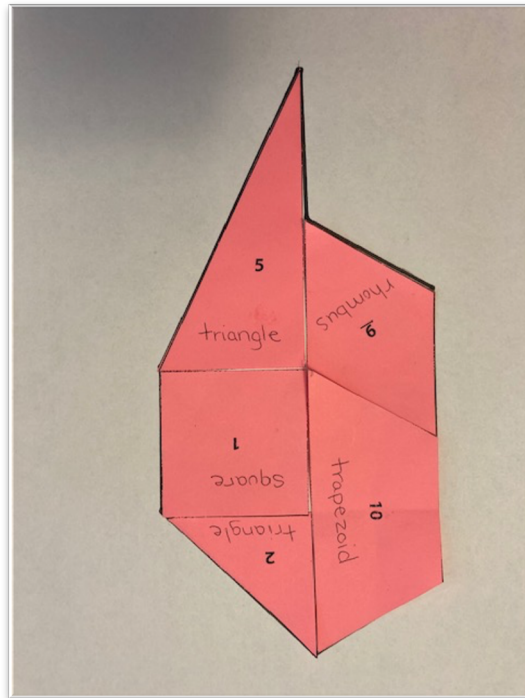


F

Note: Right triangle #5 must be flipped.



G



Create a Shape Puzzle (Shape Set)

- 1) This is a good activity to assign for homework. Students should create their own shape puzzles by putting together shapes in their shape set, and tracing the outside carefully onto paper.
- 2) Encourage students to challenge family members to solve their puzzle, and have them send you a photo so you can try to solve it too!

Square and Rhombus (page 32)

Note to teachers: A rhombus is a shape with four equal sides. Technically, a square is a special type of rhombus with right angles. Very beginning students may not be ready to grasp this relationship (all squares are rhombuses but not all rhombuses are squares). Instead, focus on getting students to notice that all the images on the page have equal sides, and that both squares and rhombuses can look like a “diamond” when angles point up and down. Have students pay attention to the way the angles change in the video.

- 1) Share the following link with students to give them a visual of how a square and a rhombus are related: Square Box <https://youtu.be/DY9ApTGiSsE>
- 2) Ask students to look at the images on the page. What do they notice? Ask them to check for equal sides, right angles, parallel lines, and lines of symmetry. You can also have them pull out the square and rhombus from their Shape Set (#1 and #9) to help with this exploration.

Compare Shapes (page 33)

This activity is similar to Triangles: Same or Different?

Dot Paper Activities Part 2

More accessible:

- 1) Try to create as many of the following shapes as you can on the triangle dot paper: rectangle, triangle, square, trapezoid, pentagon, hexagon, octagon.
 - ▶ *Which shapes were easy to make? Which were hard to make? Are there any shapes you can't make?*
- 2) Connect dots on the dot paper to make a block letter of your first initial.
- 3) Connect the dots to make a large, irregular shape, like the one in the shape puzzles. Now break the shape into smaller shapes. What types of shapes did you break it into?

More challenging:

- 1) Connect dots on the dot paper to make a block letter of your first initial. Can you break this shape up into rectangles? Triangles? A combination of both?
- 2) Connect the dots to make a large, irregular shape, like the shapes in the shape puzzles. Now break your shape up into smaller shapes. Can you break up your shape into all four sided shapes?

Shape Scavenger Hunt (page 34)

- 1) This can be assigned for homework. You can have students write where they found the examples on the page, or you could have them text you photos of what they found.
- 2) If you have multiple students on any kind of group chat, this would be a great activity to have them post their pictures for other students to see.

Sort Shapes (Page 35 & Shape Set)

- 1) This is an open-ended task. Ask the student to sort the shapes in the Shape Set into four piles, based on things that the shapes have in common. The piles do not have to be the same size. Have students tell you which shapes they placed in each pile. Then have the student give each pile a name.
- 2) **Extension:** You can do this activity again and ask them to sort into two or three piles.

Creating Shapes (page 36)

- 1) Have students use a ruler or straight edge. Explain that they should draw one or more straight lines through the hexagon. Then, they should identify the new shapes that have been created. Send students a photo of an example or two if possible. Students should break up each hexagon differently.
- 2) This is a good activity to assign for homework. Have students text you a photo of their page when they are finished.

Study Strategy (page 37)

It can be helpful to explicitly teach students ways that they can study on their own to build independence.

Common Shapes: Review (pages 38-39)

Have students fill this out with you, and check for accuracy and completeness. Review the relevant concepts they have learned so they can give an accurate description of each shape.

Is It a Rectangle? (page 40)

This activity pushes students to start to use a more formal definition to identify rectangles. In addition to deciding which shapes are rectangles, make sure they can identify which parts of the definition are violated in the shapes that are NOT rectangles.

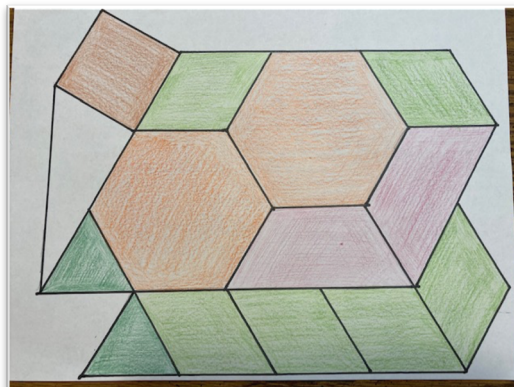
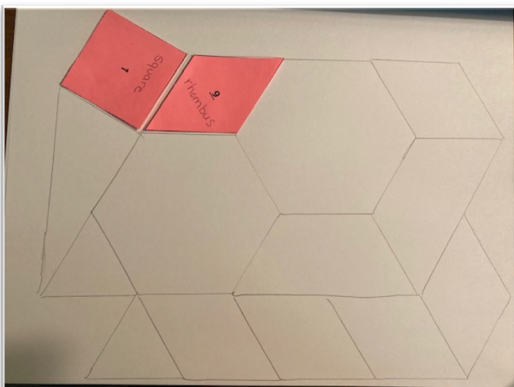
Design Challenge (page 41)

While students are looking at the design on the page, ask them the following questions:

- ▶ *What is the name of the largest shape in the design? (hexagon)*
- ▶ *What is the most frequent shape in the design? (rhombus)*
- ▶ *How many shapes share a side with the hexagon? (6)*
- ▶ *How many triangles are in this design? (3)*
- ▶ *How can you tell which shape is the square? (four equal sides, four right angles, two sets of opposite parallel sides)*
- ▶ *Of the 13 shapes in this design, how many are four-sided shapes? (9)*

Create a Design (Page 42 & Shape Set)

- 1) In this activity, students will trace shapes from the Shape Set to create a design that covers as much of a piece of paper as they can. Send them a photo of an example. The idea is to get the shapes to fit together so they cover the paper without leaving gaps. Shapes can be traced more than once.



- 2) Have students text you a photo of the design they have created. Discuss with them: Which shapes fit together well? Which ones were hard to fit?

Quiz (page 43)

The purpose of this quiz is to give students a reason to study and review what they have learned and to allow you a final opportunity to assess student mastery of the concepts.

- Name these shapes.
- Which of the shapes have right angles? How can you tell?
- Which of the shapes have parallel lines? How can you tell?
- Name one of the shapes that is symmetrical if the lines goes across the shape (horizontal).
- Give an example of somewhere you might see each of these shapes in real life.

Assessment	
Learning Objective	Where to Look for Evidence
1. Identify 6 common shapes	<ul style="list-style-type: none"> ● Design Challenge ● Quiz
2. Describe a shape's characteristics	<ul style="list-style-type: none"> ● Who Am I? ● Sort Shapes ● Quiz
3. Identify a right angle	<ul style="list-style-type: none"> ● Activities with Shape Set ● Quiz
4. Identify parallel lines	<ul style="list-style-type: none"> ● Activities with Shape Set ● Quiz
5. Identify symmetry	<ul style="list-style-type: none"> ● Symmetry activities ● Quiz
6. Give examples of where common shapes are seen in real life	<ul style="list-style-type: none"> ● Shape Scavenger Hunt ● Homework Photos ● Quiz
7. Check a shape against a definition	<ul style="list-style-type: none"> ● Is It a Rectangle?
8. Compose and decompose shapes	<ul style="list-style-type: none"> ● Create Shapes ● Shape Puzzles ● Create a Shape Puzzle ● Dot Paper Activities
9. Tech Skills: Text a photo to teacher	